Fracture toughness of zirconia nanoparticle-filled dental composites

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Abstract The fracture toughness of dental composites containing zirconia nanoparticles dispersed in a bisphenol A glycol dimethacrylate-based monomer blend (GTE) was studied for several yttria contents. Three-point bend test bars with and without a notch were tested at ambient temperature to determine elastic modulus, flexure strength, and fracture toughness. The $ZrO₂$ nanoparticles increased the fracture toughness of the nanocomposites compared to previous results for the matrix and Schott glass-filled nanocomposites. X-ray diffraction analyses revealed mostly tetragonal $ZrO₂$ in the nanocomposites before and after testing, in agreement with a theoretical analysis. The enhancement in fracture toughness in $ZrO₂$ -filled nanocomposites was caused mainly by the higher values of particle toughness and interface toughness in GTE/ $ZrO₂$ compared to those of GTE/Schott glass nanocomposites.

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Introduction

There is interest in developing dental composites reinforced with nanosized particles with near-zero volumetric shrinkage during curing and highly translucent and radiopaque post curing $[1-8]$. Other desired properties of the nanocomposites include high strength, good fracture toughness, and excellent wear resistance [\[6](#page-7-0)]. Nanosized particles are attractive fillers for dental composites because they improve composite strength and wear resistance. On the other hand, it is not obvious that nanosized particles would enhance the fracture resistance of dental nanocomposites since fracture toughness usually scales with the $\frac{1}{2}$ power of the characteristic microstructural length scale controlling the fracture process. To be an effective toughening agent, the nanosized particles must increase the process zone size at the onset of critical fracture either through an increase in the fracture strength, due to their small size scale, or the inducement of one or more new toughening mechanisms by virtue of their size scale or the large surface area-to-volume ratio.

An earlier study by the authors [\[9](#page-7-0)] demonstrated that the fracture toughness of dental composites can be enhanced using colloidal $SiO₂$ and 0.4-µm Schott glass fillers (a mixture of 50% SiO_2 , 30% BaO, 10% Al_2O_3 , and 10% B₂O₃ by weight; Schott glass GmbH, Landshut, Germany) in bisphenol A glycol dimethacrylate (bis-GMA)-based monomer blend (GTE) resin matrix, which is a 3-component monomer solution containing 37.5 wt% bis-GMA, 25 wt% triethylene glycol dimethacrylate (TEGDMA), and 37.5 wt% bisphenol A ethoxylate dimethacrylate (bis-EMA). The study [\[9](#page-7-0)] showed that the toughening ratio in these composites can be as high as 3. The dominant fracture mechanism was crack deflection by nanoparticles and interface crack propagation along the

matrix/particle interface. The sources of composite toughness enhancement were determined to be twofold: (1) interface crack growth around a particle lowers the near-tip effective stress intensity and increases the fracture toughness by about 30–60% of the matrix toughness and (2) interface toughness of matrix and silanized nanoparticles appears to be two to three times higher than that of the matrix toughness [[9\]](#page-7-0). Nanosized particles improve the overall fracture toughness by enhancing the interface bonding between the particle and matrix through a higher surface area to volume ratio. Despite a threefold increase, the fracture toughness values of the nanocomposites, which is in the range of $0.4-0.8 \text{ MPa(m)}^{1/2}$, are still low and need further improvement. On the other hand, a theoretical analysis [\[9](#page-7-0)] indicates that further increase in the interface toughness of $GTE/SiO₂$ and GTE/Schott glass nanocomposites might cause a change of the dominant fracture mechanism from interface fracture to particle fracture as the interface toughness approaches that of the particles. As a result, both the interface toughness and the particle toughness must be increased to achieve higher fracture toughness in the nanocomposites.

The objective of this article is to report the results of an investigation to improve the fracture toughness of dental nanocomposites using nanosized $ZrO₂$ fillers in GTE matrix. Zirconia nanoparticles have been selected because of a relative high fracture toughness $(2.6 \text{ MPa(m)}^{1/2} [10]$ $(2.6 \text{ MPa(m)}^{1/2} [10]$ compared to 1 MPa(m)^{1/2} for SiO₂ and Schott glass [[9](#page-7-0)]). Furthermore, nanosized spherical $ZrO₂$ particles exist in the tetragonal structure that can be induced to transform to the monoclinic structure under stress $[11, 12]$ $[11, 12]$ $[11, 12]$ $[11, 12]$, thereby providing the possibility of toughness enhancement via stress-induced transformation toughening [\[13](#page-7-0), [14](#page-7-0)]. Since the tetragonal-to-monoclinic phase transformation results in a volume increase $[11-14]$, nanosized $ZrO₂$ may also be utilized to reduce volumetric shrinkage during the curing of resin-based nanocomposites. In this article, we will first report the fabrication of the $ZrO₂$ -filled nanocomposites, followed by the experimental procedures for performing the fracture toughness tests. Experimental results of the fracture tests will be presented together with the corresponding fracture and toughening mechanisms. The experimental results indicate that $ZrO₂$ nanoparticles enhance the fracture toughness of nanocomposites without undergoing a phase transformation. The experimental results will be compared against a theoretical analysis, which shows that the tetragonal $ZrO₂$ nanoparticles are stable at the particle size range examined. The increase in fracture toughness observed in ZrO_2 -filled nanocomposites is caused mainly by a higher fracture toughness of tetragonal $ZrO₂$ compared to that of the Schott glass nanoparticles.

Experimental methods

Composite resins were formulated with a 3-component monomer solution (GTE) containing 37.5 wt% bis-GMA, 37.5 wt% bis-EMA, and 25 wt% TEGDMA (Esschem Inc., Linwood, PA). A liquid photoinitiator system comprising camphorquinone and dimethylaminoethyl methacrylate $(0.4 \text{ g}: 1.0 \text{ g})$ was added to the monomer solution at a total level of 3% (w/w) prior to formulation with fillers. $ZrO₂$ nanoparticles with an average particle size of about 12 nm, with and without yttria dopant, were selected for this study. Pure ZrO₂ nanoparticles were fabricated (ETH, Zurich, Switzerland) at 100 g/h by flame spray pyrolysis (FSP) of zirconium propoxide in ethanol solutions [\[15](#page-7-0)]. Yttria-doped zirconia nanoparticles (1–10 mol%) were made (ETH, Zurich, Switzerland) also at about 100 g/h by FSP of yttrium hexahydrate and zirconium carbonate hydroxide oxide $(Zr(OH)₂(CO3)₂·ZrO₂ = ZC, ZrO₂ content ~4.4 wt\%$, LUUnited Int'l Inc.) in acetic acid (Fluka, 99.8% AcOH), 2-ethylhexanoic acid (2-EHA, Fluka, 99%), and EtOH solutions as described by Jossen et al. [[16\]](#page-7-0). The particle size and the crystal structure were determined by X-ray diffraction (XRD) (Bruker Instruments, Model D8, Billercia, MA) and nitrogen adsorption (BET), using the procedure described earlier [\[15](#page-7-0), [16\]](#page-7-0). The resolution of the XRD was 1% yttria. Yttria formed a solid solution with the zirconia, and no separate yttria phases were present, regardless of the yttria-stabilized zirconia synthesis conditions, up to 10% yttria content [[16\]](#page-7-0).

To fabricate the nanocomposites, $ZrO₂$ particles were suspended by sonication in acetonitrile and surface treated by the addition of either diethyl (vinyl)phosphonate or diethyl(methacryloylmethyl)phosphonate. Particles were exchanged into the dental resin by centrifugation and redispersion (wet) into dichloromethane, followed by addition of the resin monomer and evaporation of the volatiles. Rectangular bar specimens 27.5 mm in length and 2 mm \times 2 mm in cross-section were fabricated by casting the composite resins into a glass mold. The specimens were pre-cured for 1 min, passing a handheld dental curing lamp (Optilux 400, Demetron Research Corp.) back and forth over the length of the specimen, to permit release from the mold. Post-curing was then performed in a halogen light box (CureLite Plus, Jeneric/Pentron, Inc.) for 10 min to assure maximum conversion of the resin.

The cured specimens were divided into two groups: (1) six flexure specimens for strength measurements and (2) six specimens for fracture toughness measurements. All six fracture toughness specimens of each composite were notched to about 0.5 mm depth at the mid span using a saw with a steel blade. Subsequently, a sharp crack was introduced at the notch tip by pressing a razor blade at the root region. Figure [1](#page-2-0) shows a sharp crack induced at the notch

Fig. 1 Three-point bend specimen of $GTE/ZrO₂$ nanocomposite with a sharp crack induced by pressing a razor blade at the notch root

root of the nanocomposites using this method. The notch tip was not controlled or measured since the induced crack tip was sharp, as shown in Fig. 1. The total crack length was measured as the sum of the notch length and the length of the sharp crack initiated from the notch.

Three-point bend tests were conducted under a displacement rate of 1 mm/min in screw-driven loading machine (Sintech, Eden Prairie, MN). Unnotched specimens were tested for elastic modulus and flexure strength, and the notched and precracked specimens were tested for fracture toughness. Six flexure specimens and six cracked specimens $(n = 6)$ were tested for each of the nanocomposites to determine the flexure strength and fracture toughness, respectively. Linear load–displacement curves were obtained for both the flexure tests and the fracture toughness tests. After testing, XRD analysis was performed (Kristalloflex 850, Siemen AG, Karlsruhe, Germany) on the center portions of the test specimens near the fracture surfaces and the outer unloaded regions to determine the crystal structure of the $ZrO₂$ nanoparticles. The microstructure of the nanocomposites was examined by atomic force microscopy (AFM; Dimension 3000, Veeco, Santa Barbara, CA). The fracture toughness values, K_{IC} , were computed on the basis of the crack length, and the maximum load at fracture according to the ASTM E399 procedure [[17\]](#page-7-0). Data were analyzed by using one-way ANOVA and post hoc Tukey comparison tests.

Results

The characteristics of the $ZrO₂$ nanoparticles and the loading level of the nanocomposites before fabrication are summarized in Table 1. Nanocomposites 1–7 were loaded to 50 wt% fillers, while Nanocomposite 8 was loaded to 31 wt% fillers. These loading levels were selected because higher loadings were not possible to achieve without reduced workability and gelation of the uncured nanocomposite. Fumed-silica fillers of a similar size to the $ZrO₂$ nanoparticles are used at levels \10 wt% in hybrid dental composites. Thus, the chosen loadings are within a relevant range for the substitution of silica in these composites.

The microstructure of $GTE/ZrO₂$ nanocomposite without yttria addition is presented in Fig. [2a](#page-3-0) and b, which shows the $ZrO₂$ as light particles in a GTE matrix at two magnifications. Figure [2b](#page-3-0) shows that the dispersion of $ZrO₂$ in the GTE matrix is not uniform microscopically and the $ZrO₂$ particles are larger than 12 nm in diameter. These larger sizes suggest that there is some agglomeration or clumping of the 12-nm diameter particles and a concentration of particles in local regions. The agglomerate particle sizes were measured from AFM images taken randomly on specimen surfaces. The average agglomerate particle size and standard deviations for Nanocomposites 1, 3, 4, and 5 after fabrication are tabulated in Table 1. The agglomerate particle sizes in these four nanocomposites are

Nanocomposite	Filler material	Filler loading $(wt\%)$	$ZrO2$ initial size (nm)	Agglomerate $ZrO2$ size in composite (nm)	$ZrO2$ structure in composite
1 (Nano ₋₁)	ZrO ₂	50	12	16.7(10.2)	Tetragonal ^a
2 (Nano \angle 2)	$ZrO2 + 7 mol% SiO2$	50	12	$\overline{}$	Tetragonal
3 (Nano $_3$)	$ZrO_2 + 2$ mol% Y_2O_3	50	12	68.2 (21.6)	Tetragonal
4 (Nano $_4$)	$ZrO_2 + 2.5$ mol% Y_2O_3	50	12	78.8 (28.9)	Tetragonal
5 (Nano_5)	$ZrO_2 + 1$ mol% Y_2O_3	50	12	27.2(10.8)	Tetragonal
6 (Nano -6)	$ZrO_2 + 1.5$ mol% Y_2O_3	50	12		Tetragonal
7 (Nano 7)	$ZrO_2 + 10$ mol% Y_2O_3	50	12		Cubic
8 (Nano_8)	$ZrO_2 + 3$ mol% Y_2O_3	31	12		Tetragonal

Table 1 A summary of the filler material, loading level, ZrO₂ particle size, and structure before and after composite fabrication

Values in parenthesis are standard deviation

^a With small amounts of monoclinic $ZrO₂$

fitted by lognormal distributions ($p \lt 0.05$), which are compared in Fig. [3.](#page-4-0) In these four cases, the agglomerate sizes of the $ZrO₂$ particles in the nanocomposites were higher than the starting particle size (12 nm) due to agglomerations of particles during the composite fabrication process [[8\]](#page-7-0). Neither the pure zirconia nor the yttriadoped zirconia nanoparticles were completely aggregated in the prepared composites, as determined by the close proximity of the XRD crystallite sizes to previously determined BET grain sizes [[15,](#page-7-0) [16\]](#page-7-0).

Results of the elastic modulus, flexure fracture strength, and fracture toughness of $GTE/ZrO₂$ nanocomposites are presented in Table [2](#page-4-0). For comparison, Table [2](#page-4-0) also presents the fracture toughness of the unfilled GTE resin and tetragonal $ZrO₂$ in bulk form and the commercial dental material Z100 (3M, Minneapolis, MN). The elastic modulus of the nanocomposites ranges from 3.74 to 4.4 MPa, while the flexure strength ranges from 71.3 to 106 MPa. For fracture toughness, the lowest value $(0.55 \text{ MPa(m)}^{1/2})$ was observed in the $ZrO₂$ nanocomposite without yttria addition and the highest value $(0.86 \text{ MPa(m)}^{1/2})$ was observed in $ZrO₂$ nanocomposites with 10% yttria. XRD results indicated that pure $ZrO₂$ particles or slightly doped ones with yttria $(\leq 3 \text{ mol\%)}$ were mostly tetragonal before [\[18](#page-7-0)] and after fracture tests for Nanocomposites 1–6. Typical results for Nanocomposite 4 before and after fracture testing are shown in Fig. [4a](#page-4-0) and b, respectively. Among these materials, monoclinic $ZrO₂$ in very small

Fig. 3 Distributions of agglomerate $ZrO₂$ particle size in four $ZrO₂$ / GTE nanocomposites

amounts were detected only in $ZrO₂$ nanocomposites without yttria addition (Nanocomposite 1). Nanocomposites 7 and 8 showed cubic $ZrO₂$ particles before and after fracture tests. In all cases, the $ZrO₂-filled$ nanocomposites exhibit a statistically higher ($p < 0.05$) fracture toughness than Z100, which was used as a control, and the GTE resin.

The fracture mechanisms in the nanocomposites were identified by fractographic examination in a 3D digital microscope (Keyence, Model VHX-100, Woodcliff, NJ). At low magnifications $(x1,000)$, the fracture surfaces in the nanocomposites were typically very flat. At higher magnifications $(x4,000)$, the fracture surfaces exhibited numerous circular features that were about $1 \mu m$ in diameter and larger ones at 3–4 μ m in diameter, as shown in Fig. [5](#page-5-0)a. A surface height map of these features, shown in

Fig. 4 X-ray diffraction results indicate the presence of tetragonal $ZrO₂$ (JCPDF card no. $\langle 17-093 \rangle$ [\[23\]](#page-7-0)) in the nanocomposite before and after fracture testing: a Before fracture test. b After fracture test

Table 2 A summary of the elastic modulus, fracture stress, and fracture toughness of GTE/ZrO₂ nanocomposites

Nanocomposite	Filler material	Filler loading $(wt\%)$	Elastic modulus (GPa)	Fracture stress (MPa)	Fracture toughness $(MPa(m)^{1/2})$
1 (Nano ₋₁)	ZrO ₂	50	4.14(0.18)	97.41 (12.9)	0.55(0.08)
2 (Nano 2)	$ZrO_2 + 7$ mol% SiO ₂	50	3.74(0.20)	71.3(25.5)	0.70(0.18)
3 (Nano 3)	$ZrO_2 + 2$ mol% Y_2O_3	50	4.02(0.38)	106.0(10.8)	0.77(0.11)
4 (Nano 4)	$ZrO_2 + 2.5$ mol% Y_2O_3	50	4.04(0.16)	96.8 (22.8)	0.79(0.17)
5 (Nano -5)	$ZrO_2 + 1$ mol% Y_2O_3	50	4.40(0.26)	93.9 (17.0)	0.76(0.11)
6 (Nano 6)	$ZrO_2 + 1.5$ mol% Y_2O_3	50	3.97(0.25)	73.4 (33.0)	0.79(0.12)
7 (Nano 7)	$ZrO_2 + 10$ mol% Y_2O_3	50	4.18(0.15)	86.2 (16.8)	0.86(0.12)
8 (Nano 8)	$ZrO_2 + 3$ mol% Y_2O_3	31			0.80(0.17)
GTE resin	Unfilled	Ω	2.90(0.14)	123.3(4.02)	0.22(0.06)
Z ₁₀₀	N.A.	N.A.	17.76 (3.44)	136.34 (32.90)	0.44(0.08)
$ZrO2$ [10, 11]	N.A.	N.A.			2.6(0.52)

The ZrO₂-filled nanocomposites exhibit a statistically higher ($p < 0.05$) fracture toughness than the control (Z100) and the GTE resin Values in parenthesis are standard deviation

Fig. 5 3D digital images of the fracture surface of Nanocomposite 4 (Nano_4) showing: a Numerous circular features $1 \mu m$ in diameter and some circular features at $3-4$ µm in diameter. **b** A surface height profile indicating the presence of hills (light) and valleys (dark) on the fracture surface. The hills correspond to particles sticking out on the surface, while the valleys (dark) indicate holes created by particles being pulled out from the fracture surface

Fig. 5b, indicated that some of the circular features were particles (light) sticking out on the surface, while others (dark) were holes or depressions. These observations suggested that based on their size, clumps of $ZrO₂/GTE$ composite particles were pulled out from the fracture surfaces, creating holes (dark) on the fracture surface. On the same surface, individual clumps of composite particles (light) were visible on the fracture surface (Fig. 5b). Similar results were observed in other nanocomposites [\[9](#page-7-0)]. These results are consistent with the AFM observations that $ZrO₂$ nanoparticles often occur in clumps in the nanocomposites. However, the particles and voids observed on the fracture surfaces were at least ten times larger than the largest agglomerated particle sizes shown in Fig. [3.](#page-4-0) Thus, the observation suggests that the fracture mechanism involved crack deflection around clumps of $ZrO₂$ particles and pullout of composite clumps that contained both $ZrO₂$ agglomerate particles and the GTE matrix.

The fracture toughness data of $GTE/ZrO₂$ nanocomposites are compared against those of GTE/colloidal $SiO₂/$ Schott glass from an earlier study [[9\]](#page-7-0) in Fig. 6, which

Fig. 6 Fracture toughness of $GTE/ZrO₂$ nanocomposites compared to GTE/Schott glass nanocomposites from Chan et al. [\[9\]](#page-7-0): a As a function of weight percent particles. b As a function of volume percent particles

shows the fracture toughness values as a function of volume fraction of the nanoparticles in the composites. The comparison indicates that ZrO_2 -filled nanocomposites are more fracture resistant than those containing silica nanoparticles. For both types of composites, the fracture mechanisms are predominantly crack deflection by nanoparticles [\[9](#page-7-0)]. The higher fracture toughness observed in $GTE/ZrO₂$ nanocomposites appears to originate from crack deflection by the $ZrO₂$ fillers in a tortuous crack path around the clumps of particles and along the matrix/particle interface, as suggested by the fractographic observations in Fig. 5. For a deflected crack advancing on the particle/ matrix interface, the fracture toughness of the nanocomposites arises from contributions of the matrix and interface toughness, and is given by [[9,](#page-7-0) [19\]](#page-7-0)

$$
K_{\rm C} = \left[1 + \alpha_{\rm tl} \alpha_{\rm pr} \left(\frac{K_{\rm in}}{K_{\rm m}}\right)^2\right]^{1/2} K_{\rm m} \tag{1}
$$

where K_{in} is the interface toughness, K_{in} is the fracture toughness of the matrix, α_{tl} is the toughness parameter for deflection of tilted cracks, and $\alpha_{\rm pr}$ is the toughness parameter for crack deflection by an interface crack advancing from the pole and around spherical particles. The values of α_{tl} and α_{pr} are 0.87 and 1.6, respectively [\[9](#page-7-0)]. Using $K_m = 0.22 \text{ MPa(m)}^{1/2}$ for the GTE resin matrix and assuming $K_{\text{in}}/K_{\text{m}} = 9$, Eq. [1](#page-5-0) is applied to correlate the fracture toughness of $GTE/ZrO₂$ composites. The calculated curve (solid line) is compared against experimental data for $GTE/ZrO₂$ composites from this study. The comparison showed that $K_{\text{in}}/K_{\text{m}} = 9$ overpredicted the fracture toughness values of $GTE/ZrO₂$ nanocomposites at the 50% loading level, suggesting that the $K_{\text{in}}/K_{\text{m}}$ value for these nanocomposites is \leq 9. Figure [6](#page-5-0) also shows a comparison of $GTE/ZrO₂$ results against those of $GTE/Schott$ glass particles from a previous study [\[9](#page-7-0)]. For GTE/Schott glass particles, the increase in fracture toughness with increasing filler contents is well described by Eq. [1](#page-5-0) using a $K_{\text{in}}/K_{\text{m}}$ ratio of 3 and $K_m = 0.22 \text{ MPa(m)}^{1/2}$, which is shown as the dashed line in Fig. [6.](#page-5-0) In contrast, the experimental data from $GTE/ZrO₂$ nanocomposites at the 50% loading level is above the dashed line $(K_{in}/K_m = 3)$ but below the solid line $(K_{in}/K_{m} = 9)$. The comparison of these two sets of experimental data and calculated curves revealed that the fracture toughness of $GTE/ZrO₂$ nanocomposites are higher than those of GTE/Schott glass at a given volume fraction or loading level of nanoparticles by virtue of a high $K_{\text{in}}/K_{\text{m}}$ ratio (3 $\le K_{\text{in}}/K_{\text{m}} \le 9$) resulting from better interface bonding between the matrix and the nanoparticles. The fracture toughness (K_{IC}) of fully established cubic $ZrO₂$ determined by fracture mechanics specimens is 2.8 MPa(m)^{1/2}, while it ranges from 5 to 6.5 MPa(m)^{1/2} for partially stabilized tetragonal $ZrO₂$ [[20\]](#page-7-0). The higher fracture toughness values in the partially stabilized tetragonal $ZrO₂$ are due to the presence of transformation toughening during the fracture process. For tetragonal $ZrO₂$ in the absence of transformation toughness, the fracture toughness (K_{IC}) determined by the Vickers indentation method is 2.6 MPa(m)^{1/2} [[9\]](#page-7-0), while it is 2.8 \pm 0.14 MPa(m)^{1/2} for cubic $ZrO₂$ [\[11](#page-7-0)]. A direct comparison [\[21](#page-7-0)] of Vickers indentation fracture toughness (K_{IV}) and standard fracture toughness (K_{IC}) determined using fracture mechanics specimens such as single-edge-notched beam and double cantilever beam indicated that the two methods produced comparable results within the $\pm 20\%$ experimental scatters. Thus, the fracture toughness of $ZrO₂$ particles is at least 2.6 ± 0.52 MPa(m)^{1/2} and may be higher if transformation toughness occurs. In comparison, the fracture toughness of Schott glass particles is about 1 MPa $(m)^{1/2}$. The higher fracture toughness established by $GTE/ZrO₂$ nanocomposites can therefore be attributed to a higher fracture

toughness of the $ZrO₂$ particles and a higher interface toughness or $K_{\text{in}}/K_{\text{m}}$ ratio. It also appears that the higher fracture toughness of the $ZrO₂$ particles give rise to higher interface fracture toughness values $(0.8-1.8 \text{ MPa(m)}^{1/2})$ and the corresponding ranges of the K_{in}/K_{m} ratio (3 $\le K_{in}/K_{in}$) $K_m \leq 9$) so that the sizes of the pullout composite particles are more than ten times larger than the sizes of the agglomerate $ZrO₂$ particles.

Discussion

The results of this investigation clearly showed that the tetragonal $ZrO₂$ nanoparticles did not transform to the monoclinic structure during fracture testing. Thus, transformation toughening can be ruled out as a source of the toughness enhancement in the $GTE/ZrO₂$ nanocomposites. To understand the absence of transformation toughening in the $ZrO₂$ -filled composites, the theoretical analysis by Suresh et al. [[22\]](#page-7-0) for stress-free transformation was modified to define the crystalline size and yttria content required for triggering the onset of stress-induced phase transformation in zirconia $[11-14]$. The theoretical model is a thermodynamic model that takes into account the free energy change associated with the transition of $ZrO₂$ from the tetragonal-to-monoclinic structure, the surface energy of the nanosized particles, the elastic strain energy, and the presence of an external stress [[12–14\]](#page-7-0). For spherical particles, the critical particle diameter (d^*) for the transformation of tetragonal-to-monoclinic $ZrO₂$ is given by [[22\]](#page-7-0)

$$
d^* = \frac{-10(\Delta h_{\text{surf}} - T\Delta S_{\text{surf}})}{\Delta H_{\text{vol}} - T\Delta S_{\text{vol}} - \sigma_{\text{c}}\theta^{\text{T}}}
$$
(2)

where Δh_{surf} and ΔS_{surf} are the enthalpy and entropy change associated with the surface energy difference of the tetragonal-to-monoclinic transformation of nanosized ZrO_2 , respectively; ΔH_{vol} and ΔS_{vol} are the enthalpy and entropy change associated with the volume free energy change of tetragonal-to-monoclinic transformation of infinitely sized $ZrO₂$, respectively; T is absolute temperature; σ_c is the transformation stress; and θ^T is the volume change associated with the tetragonal-to-monoclinic transformation. The $\sigma_c\theta^T$ term [[11–14\]](#page-7-0) accounts for the presence of stress during the phase transformation process.

Using the thermodynamic data [\[22](#page-7-0)] in the literature, the theoretical model was utilized to compute the critical crystalline size for the transition from tetragonal-tomonoclinic $ZrO₂$ as a function of yttria content. The transformation stress was taken to be 0 (stress-free transformation), 250, and 500 MPa and θ ^T \approx 0.04 [\[14](#page-7-0)]. The theoretical results are compared against experimental data [\[10](#page-7-0), [11\]](#page-7-0) and theoretical results of Suresh et al. [\[22](#page-7-0)] in

Fig. 7 Calculated critical crystalline $ZrO₂$ diameter for the tetragonal-to-monoclinic transformation at three stress levels as a function of yttria content compared to experimental data from the literature $[10, 11]$ and this study

Fig. 7. Figure 7 shows that the critical crystalline size increases with increasing yttria contents. The presence of an external stress reduces the critical crystalline size at a given level of yttria content. Below the critical crystalline size, $ZrO₂$ is stable in the tetragonal form, but it can transform to monoclinic under stress-free conditions when the crystalline size exceeds the critical size (solid line). The critical size is reduced by an external stress, as shown in Fig. 7. For $GTE/ZrO₂$ nanocomposites studied, the sizes of the $ZrO₂$ nanoparticles are below the critical sizes required for the phase transformation to occur. Thus, the tetragonalto-monoclinic transformation is energetically unfavorable; hence, the absence of transformation toughening in the $ZrO₂$ -filled nanocomposites can be understood on the basis that the tetragonal $ZrO₂$ nanoparticles are overly stabilized. To induce transformation toughening, the size of the $ZrO₂$ nanoparticles must be increased or the yttria content must be decreased to just below the critical size boundary (solid line) so that the tetragonal-to-monoclinic transformation can occur under the assistance of an external stress.

Conclusions

The conclusions reached, based on the results of this investigation, are as follows:

- 1. $ZrO₂$ nanoparticles increased the fracture toughness of the nanocomposites compared to the matrix alone and those containing silica-nanoparticle fillers.
- 2. The fracture mechanisms in $GTE/ZrO₂$ nanocomposites include crack deflection by particles and fracture along the matrix/particle interface.
- 3. Transformation toughening is absent in nanoparticlefilled GTE because the $ZrO₂$ nanoparticles favor the tetragonal structure in the ranges of particle sizes and yttria contents examined. The particle size needs to be increased to induce transformation toughening.
- 4. The fracture toughness in $GTE/ZrO₂$ nanocomposites originates from the interface toughness, crack deflection, and a higher inherent fracture toughness of the $ZrO₂$ nanoparticles as compared to silica nanoparticles.

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References

- 1. Furman B, Rawls HR, Wellinghoff ST, Dixon H, Nicolella D (2000) Crit Rev Biomed Eng 28:439
- 2. Rawls HR, Furman B, Wellinghoff ST, Nicolella D, Dixon H, Ong JL, Park Y-J, Norling GK (2000) J Korean Res Soc Dent Mater 27:3
- 3. Park Y-J, Chae K-H, Rawls HR (1999) Dent Mater 15:120
- 4. Chan DCN, Titus HW, Chung KH, Dixon H, Wellinghoff ST, Rawls HR (1999) Dent Mater 15:219
- 5. Rawls HR, Wellinghoff VT, Norling BK, Leamon SH, Swynnerton NF, Wellinghoff ST (1997) ACS Polym Prepr 38(2):167
- 6. Wellinghoff ST, Dixon H, Nicolella DP, Norling BK, Rawls HR (1998) Metal oxide nanoparticle-polymer composites: structure property relationships, dental, and other applications. In: Fine, ultrafine and nano powders. Business Communication, Norwalk
- 7. Schulz H, Madler L, Pratsinis SE, Burtscher P, Mozner N (2005) Adv Funct Mater 15(5):830
- 8. Schulz H, Pratsinis SE, Rüegger H, Zimmermann J, Klapdohr S, Salz U (2008) Colloid Surf A 315:79. doi[:10.1016/j.colsurfa.](http://dx.doi.org/10.1016/j.colsurfa.2007.07.016) [2007.07.016](http://dx.doi.org/10.1016/j.colsurfa.2007.07.016)
- 9. Chan KS, Nicolella DP, Furman BR, Lee Y-D, Wellinghoff S, Rawls R (2007) Eng Fract Mech 74:1857
- 10. Bravo-Leon A, Morikawa Y, Kawahara M, Mayo MJ (2000) Acta Mater 50:4555
- 11. Lange FF (1982) J Mater Sci 17:240. doi:[10.1007/BF00809059](http://dx.doi.org/10.1007/BF00809059)
- 12. Evans AG, Cannon RM (1986) Acta Metall 34(5):761
- 13. McMeeking RM, Evans AG (1982) J Am Ceram Soc 65:242
- 14. Zeng D, Katsube N, Soboyejo WO (2004) Mech Mater 36:1057
- 15. Mueller R, Jossen R, Pratsinis SE, Watson M, Akhtar MK (2004) J Am Ceram Soc 87:197
- 16. Jossen R, Mueller R, Pratsinis SE, Watson M, Akhtar MK (2005) Nanotechnology 16:S609
- 17. ASTM E399-90 (1999) Annual book of ASTM standards, vol 03.01. ASTM, West Conshohocken, p 422
- 18. Jossen R, Heine MC, Pratsinis SE, Akhtar MK (2006) CVD J 12:614
- 19. Faber KT, Evans AG (1983) Acta Metall 31:565
- 20. Liu AF (2005) Mechanics and mechanisms of fracture: an introduction. ASM International, Materials Park, p 298
- 21. Matsumoto RLK (1987) J Am Ceram Soc 70(12):C-366
- 22. Suresh A, Mayo MJ, Porter WD (2003) J Mater Res 18:2912
- 23. Joint Committee on Powder Diffraction Files, International Center for Diffraction Data, Swarthmore, PA, 1992